## 5. Recombination

## Problems

5.1. A semiconductor with an intrinsic carrier concentration of  $n_i = 4.8 \times 10^8 \text{ cm}^{-3}$  is doped with an acceptor density of  $N_A = 3.0 \times 10^{17} \text{ cm}^{-3}$ :

a) In equilibrium, find:

i) The density of holes  $(p_0)$  and electrons  $(n_0)$ .

ii) The separation of the Fermi level from the intrinsic energy ( $E_i - E_F$ ).

b) The material is now uniformly illuminated, which generates carrier by band-to-band photoexcitation at a rate  $G = 2.5 \times 10^{10} \text{ cm}^{-3} \text{s}^{-1}$ . Assume the coefficient of radiative recombination is  $B_{\text{rad}} = 6.2 \times 10^{-10} \text{ cm}^3 \cdot \text{s}^{-1}$ .

- i) Compute the radiative recombination lifetime for electrons  $\tau_{n,rad}$ .
- ii) In steady state, the radiative recombination rate  $U_{rad}$  equals the generation rate. Find the density of photogenerated carriers (the excess carrier density) in steady state  $\Delta n = \Delta p$ .
- iii) Find the Fermi-level splitting  $\Delta \mu$ .
- iv) Find the shift of the electron quasi-Fermi level ( $E_{F_n} E_F$ ).

c) Now a region of the material is illuminated that also contains traps with a density  $N_t = 3.0 \times 10^{14} \text{ cm}^{-3}$ , but with otherwise identical properties to the material analyzed in a) and b). Assume  $B_n = 2.8 \times 10^{-7} \text{ cm}^3 \cdot \text{s}^{-1}$ ,  $B_p = 4.8 \times 10^{-7} \text{ cm}^3 \cdot \text{s}^{-1}$ , and  $E_i - E_t = 0.241 \text{ eV}$ .

- i) Find the capture lifetime for electrons  $\tau_{n,\text{SRH}}$  and holes  $\tau_{p,\text{SRH}}$ .
- ii) Find the carrier densities  $n_t$  and  $p_t$  when the Fermi level is at the trap level.
- iii) The net recombination rate  $U = U_{rad} + U_{SRH}$  equals the generation rate in steady state. Estimate the excess carrier density  $\Delta n$  with both recombination mechanisms present.
- iv) Find the shift  $E_{F_n} E_F$  of the electron quasi-Fermi level.

d) Assume the Auger-recombination coefficient for electrons in p-type material is

 $A_n = 1.2 \times 10^{-27} \text{ cm}^6 \cdot \text{s}^{-1}$ . Find:

i) The Auger lifetime for electrons  $\tau_{n,Aug}$ .

- ii) The excess carrier density  $\Delta n$  with all three recombination mechanisms present.
- iii) The shift  $E_{F_n} E_F$  of the electron quasi-Fermi level.